

# Regular parallelisms in terms of the Klein quadric

*Introduce:*

**Silvia PIANTA**

Università Cattolica del Sacro Cuore

*Interviene:*

**Hans HAVLICEK**

Vienna University of Technology

Over any field  $K$ , there is a bijection between regular spreads of the projective space  $PG(3, K)$  and external lines to the Klein quadric in  $PG(5, K)$ . Under this bijection, the set of parallel classes of any regular parallelism of  $PG(3, K)$  corresponds to a set of lines, say  $H$ , that determines a *hyperflock* of the Klein quadric, that is, a partition of the Klein quadric by elliptic subquadrics. Such an  $H$  is therefore called a *hyperflock determining line set* or an "hfd line set" for short. We report on some of the known examples of hfd line sets and their corresponding parallelisms.

An hfd line set is said to be *pencilled* if it is composed of pencils of lines. We present a construction of pencilled hfd line sets and outline the rather intricate proof that this construction determines all hfd line sets.

Among the regular parallelisms of  $PG(3, K)$  that correspond to pencilled hfd line sets are all its Clifford parallelisms. This observation allows us to derive necessary and sufficient algebraic conditions on the ground field  $K$  that guarantees the existence of pencilled hfd line sets.

## Seminario

**Venerdì 13 aprile 2018**

**Sala Riunioni, ore 11.00**

Via dei Musei 41 - Brescia

