

# Effetti quantistici alla basse temperature: dalla supercondutività alla superfluidità

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PERCORSI INNOVATIVI  
in Matematica e in Fisica

Conferenze



UNIVERSITÀ  
CATTOLICA  
del Sacro Cuore



C. Giannetti

Montichiari 2 Aprile 2014



# Effetti quantistici alla basse temperature: dalla superconduttività alla superfluidità

- Condensazione di Bose-Einstein
- Superfluidità
- Superconduttività

meccanica quantistica  
nel mondo macroscopico!



# Nobel Prizes in Physics



The Official Web Site of the Nobel Prize

•1913: H. Kamerlingh Onnes

"for his investigations on the properties of matter at low temperatures which led, inter alia, to the production of liquid helium"



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for the creation of Quantum Mechanics and the discovery of the wave nature of matter

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"for his theoretical predictions of the properties of a supercurrent through a tunnel barrier, in particular those phenomena which are generally known as the Josephson effects"
- 1972: J. Bardeen, L.N. Cooper, R. Schrieffer  
"for their jointly developed theory of superconductivity, usually called the BCS-theory"
- 1962: Lev Landau  
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# Nobel Prizes in Physics

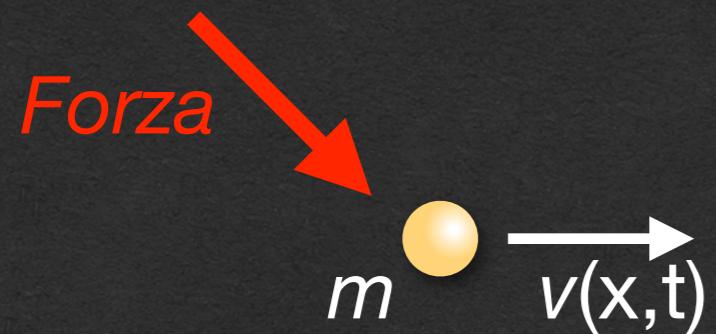


The Official Web Site of the Nobel Prize

- 2003: A.A. Abrikosov, V.L. Ginzburg, A.J. Leggett  
"for pioneering contributions to the theory of superconductors and superfluids"
- 2001: E.A. Cornell, W.Ketterle, C.E. Wieman  
"for the achievement of Bose-Einstein condensation in dilute gases of alkali atoms, and for early fundamental studies of the properties of the condensates"
- 1997: S. Chu, C. Cohen-Tannoudji, W.D. Phillips  
"for development of methods to cool and trap atoms with laser light"
- 1996: D.M. Lee, D.D. Osheroff, R.C. Richardson  
"for their discovery of superfluidity in helium-3"
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fisica classica



equazione del moto:

$$\vec{F} = m \vec{a}$$

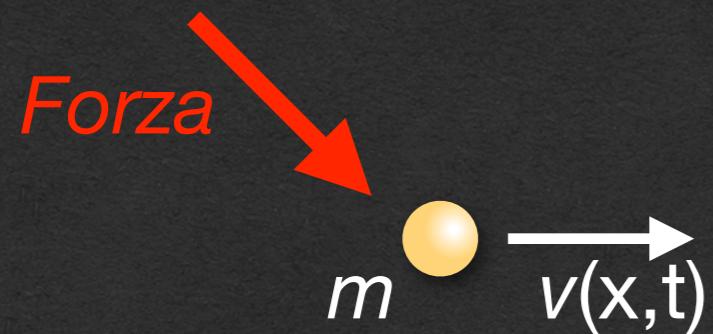
accelerazione

$$\vec{a} = \frac{d\vec{v}}{dt}$$



# il mondo quantistico

fisica classica



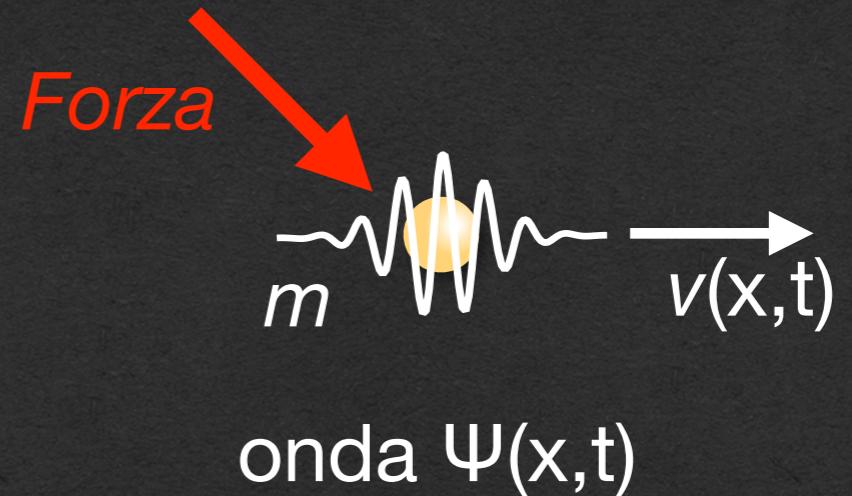
equazione del moto:

$$\vec{F} = m \vec{a}$$

accelerazione

$$\vec{a} = \frac{d\vec{v}}{dt}$$

meccanica quantistica



equazione di Schroedinger:

$$-\frac{\hbar^2}{2m} \frac{d^2\Psi}{dx^2} + V\Psi = E\Psi$$

forze esterne

energia

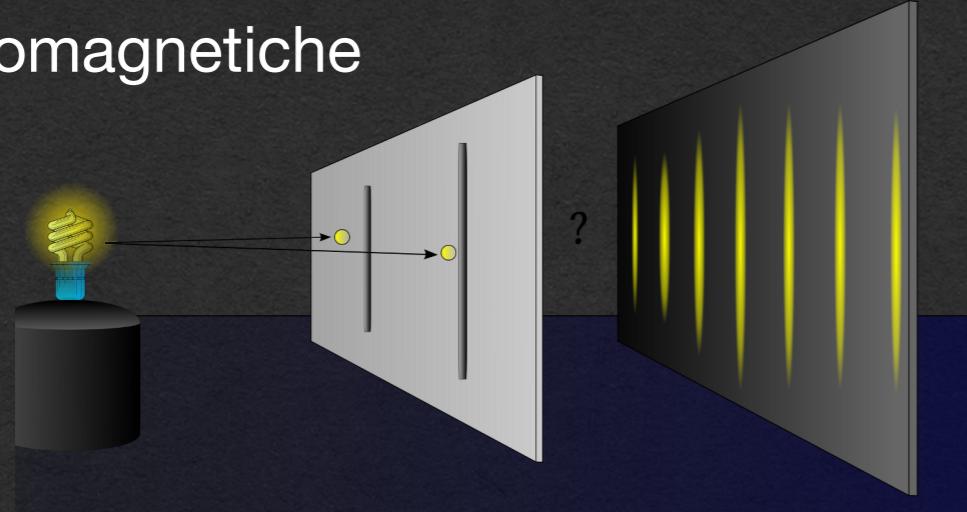


# il mondo quantistico

## interferenza tra onde



onde  
elettromagnetiche

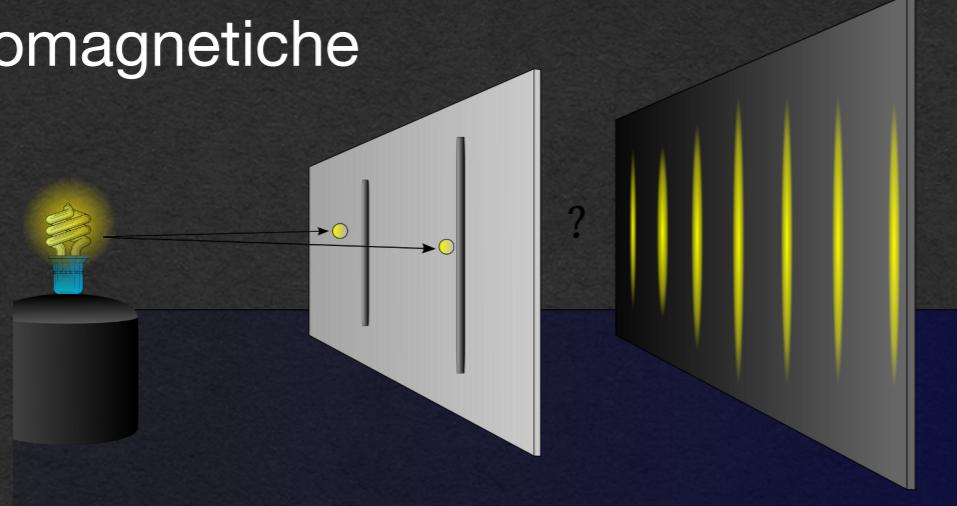


# il mondo quantistico

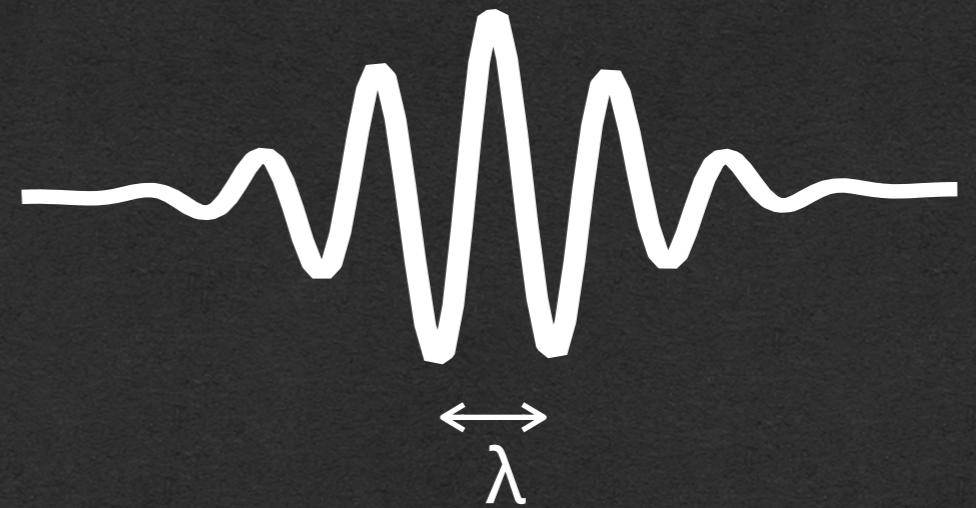
## interferenza tra onde



onde  
elettromagnetiche



## onda di materia



lunghezza d'onda  
di De Broglie:

$$\lambda_{DB} = \frac{h}{mv}$$

costante di  
Planck

$\sim 1 \text{ nm}$  @ elettrone con  $v=5000 \text{ Km/s}$

$\lambda_{DB}=$

$\sim 10^{-14} \text{ nm}$  @ massa ad 1 mg  
con  $v=5000 \text{ Km/s}$



- 
- Condensazione di Bose-Einstein  
(predetta nel 1925 → scoperta in atomi alkalini nel 1995)
  - Superfluidità
  - Supercondutività



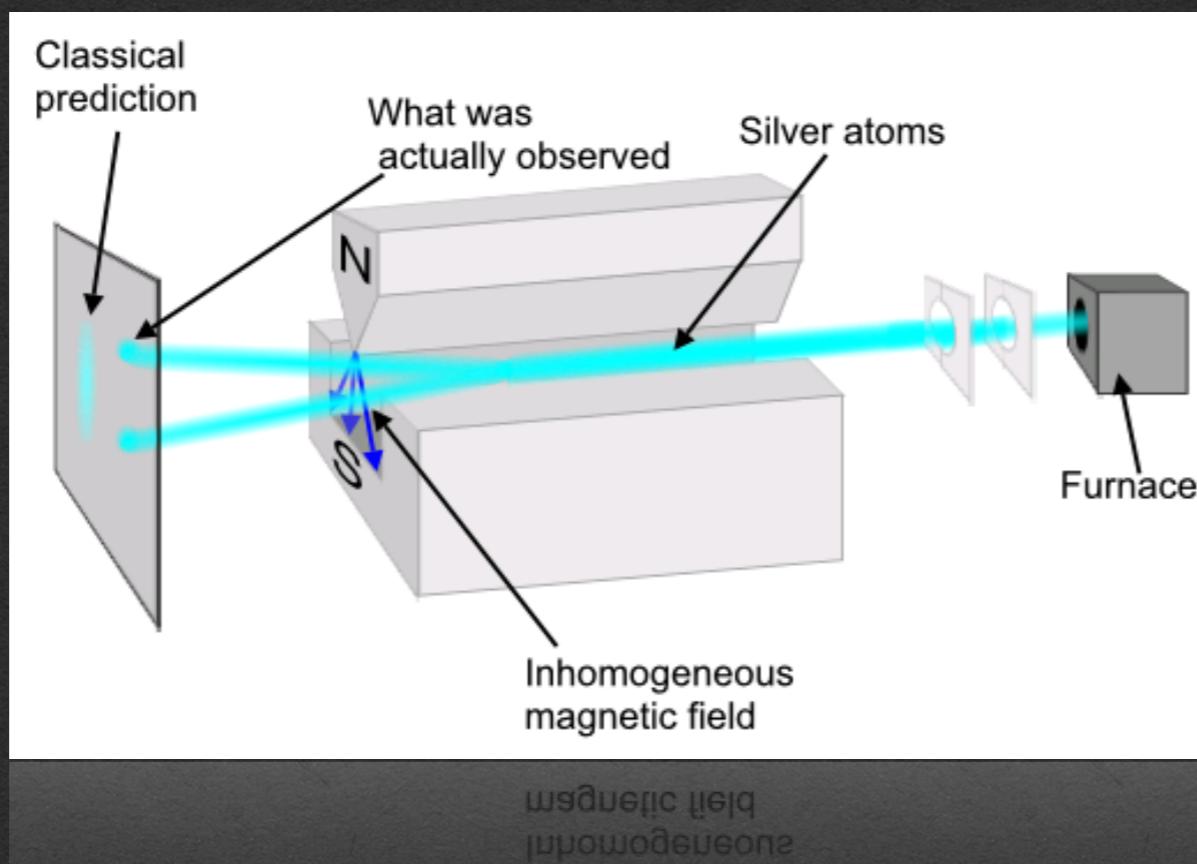
# Condensazione di Bose-Einstein

## effetto macroscopico della statistica di Bose-Einstein

**BOSONE** = particella spin intero (fotone, fonone, atomi alkali, bosone di Higgs, ecc.)

**FERMIONE** = particella spin semi-intero (elettrone, protone, ecc.)

esperimento di Stern-Gerlach (1922)

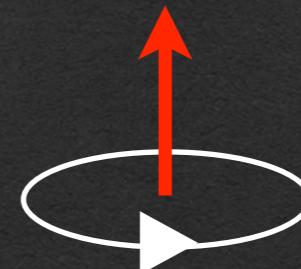


### particella quantistica

- elettrone:  $S=1/2$
- atomi:  $J_{\text{tot}}$  (momento magnetico totale)



### analogo classico

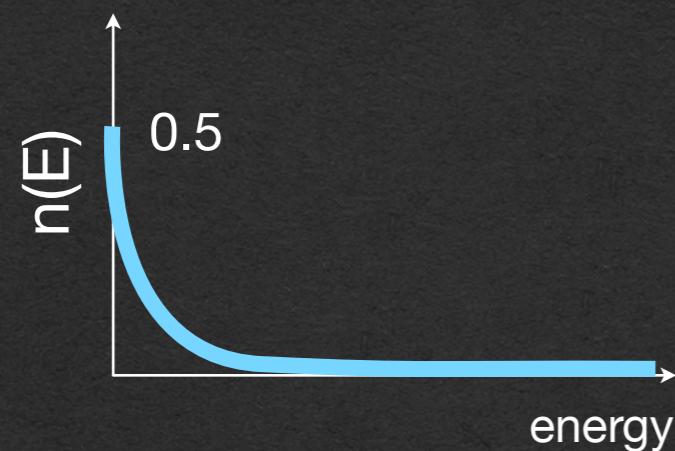


momento magnetico di un circuito percorso da corrente

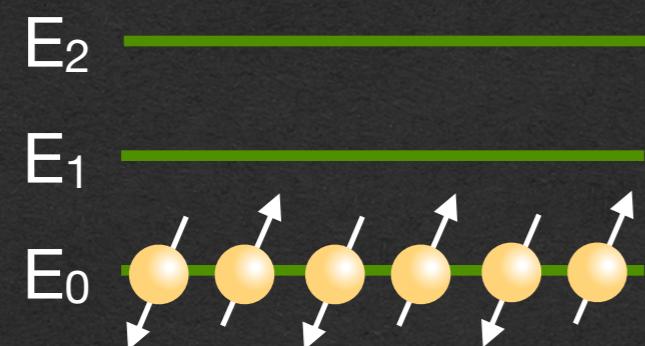


# statistiche quantistiche

Bose-Einstein distribution

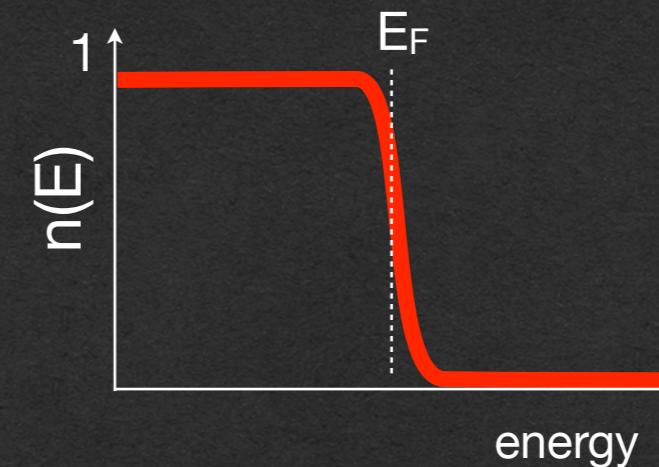


bosoni

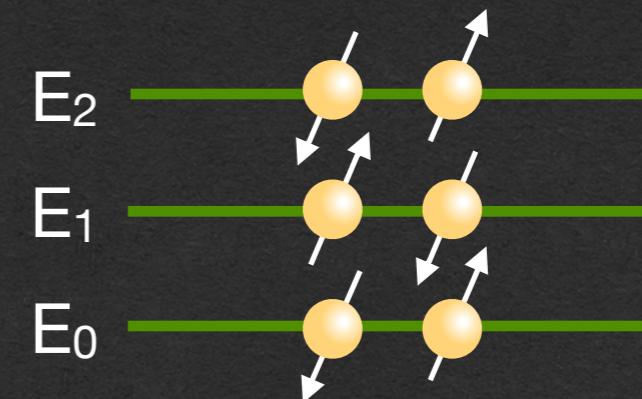


Condensazione di Bose-Einstein  
predetta nel 1925 da A. Einstein

Fermi-Dirac distribution



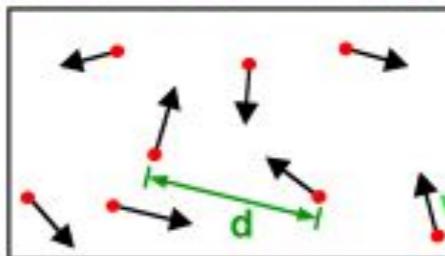
fermioni



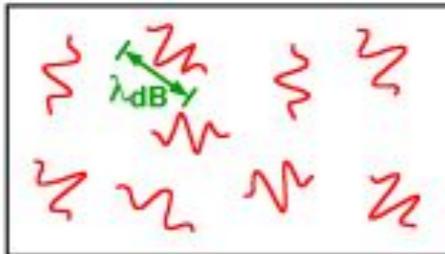
# condensazione di Bose-Einstein

W. Ketterle Nobel Lecture 2001

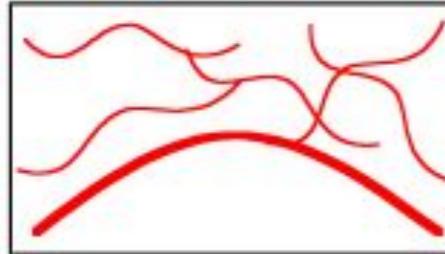
## What is Bose-Einstein condensation (BEC)?



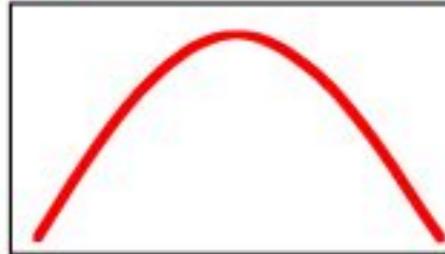
**High Temperature T:**  
thermal velocity  $v$   
density  $d^{-3}$   
"Billiard balls"



**Low Temperature T:**  
De Broglie wavelength  
 $\lambda_{dB} = h/mv \propto T^{-1/2}$   
"Wave packets"



**$T=T_{crit}$ :**  
Bose-Einstein  
Condensation  
 $\lambda_{dB} = d$   
"Matter wave overlap"



**$T=0$ :**  
Pure Bose  
condensate  
"Giant matter wave"

"Giant matter wave"  
condensate  
at zero  
temperature

energia  
cinetica  
particella

$$\frac{1}{2}mv^2 = \frac{3}{2}K_B T$$

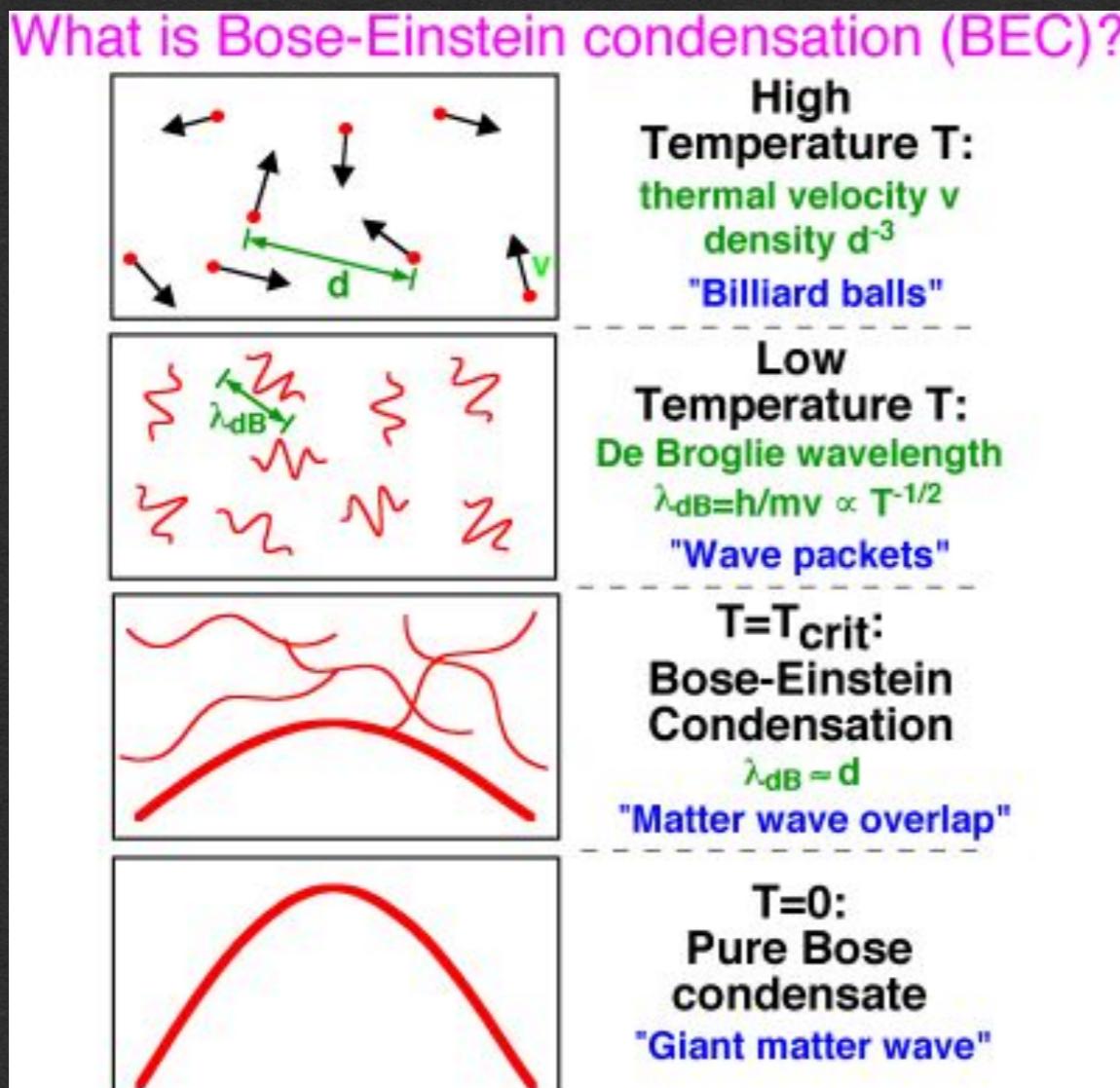
energia  
termica

classicamente:



# condensazione di Bose-Einstein

W. Ketterle Nobel Lecture 2001



classicamente:

$$\frac{1}{2}mv^2 = \frac{3}{2}K_B T$$

energia cinetica particella      energia termica

lunghezza d'onda di de Broglie:

cost. Planck

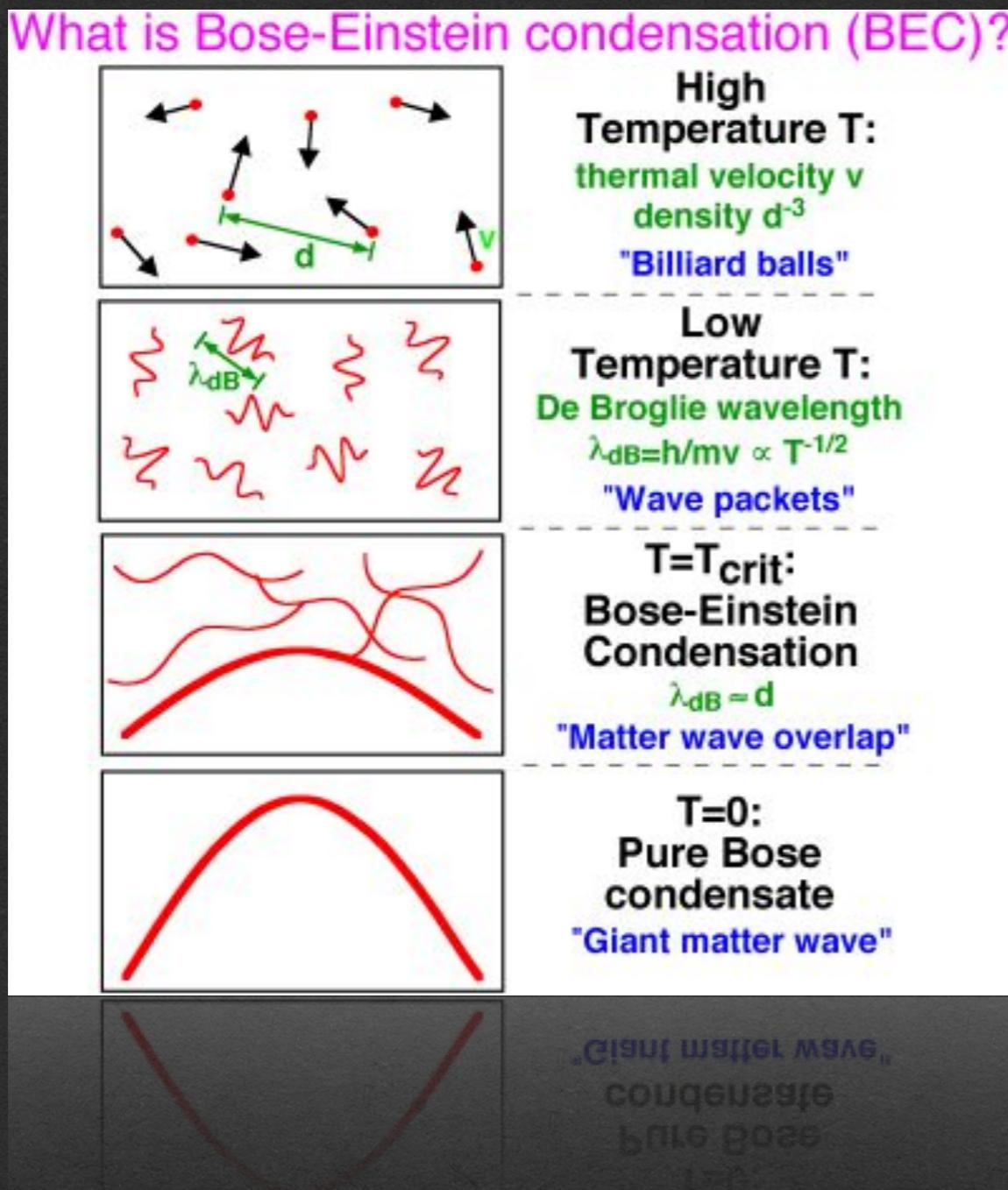
$$\lambda_{DB} = \frac{h}{mv} \propto \frac{1}{\sqrt{T}}$$

"Giant matter wave"  
condensate  
at same time



# condensazione di Bose-Einstein

W. Ketterle Nobel Lecture 2001



classicamente:

$$\frac{1}{2}mv^2 = \frac{3}{2}K_B T$$

energia cinetica particella      energia termica

lunghezza d'onda di de Broglie:

cost. Planck

$$\lambda_{DB} = \frac{h}{mv} \propto \frac{1}{\sqrt{T}}$$

temperatura di condensazione:

$$T_c = \frac{2\pi\hbar^2}{k_B m} \left( \frac{n}{2.6} \right)^{2/3}$$

densità  
massa della particella



# bosoni nella tavola degli elementi

$^4\text{He} \rightarrow J=0$

T<sub>c</sub>=3.1 K

in 1913 liquefazione  
di  ${}^4\text{He}$  a  $T \approx 4$  K  
K. Onnes (Nobel Prize)

ma atomi fortemente  
interagenti!!



# bosoni nella tavola degli elementi

## atomi alkalini

$T_c = 10 \text{ nK} - 1 \mu\text{K}$

ma atomi  
debolmente  
interagenti!!

## $^4\text{He} \rightarrow J=0$

T<sub>c</sub>=3.1 K

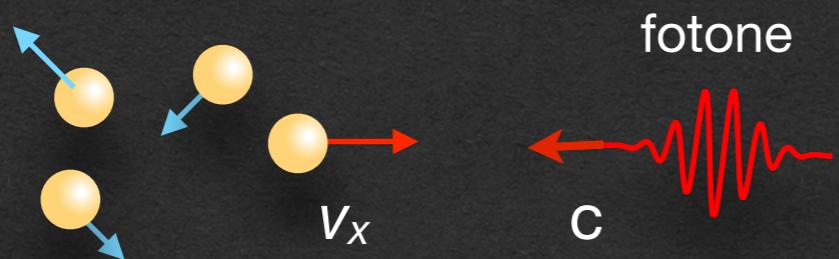
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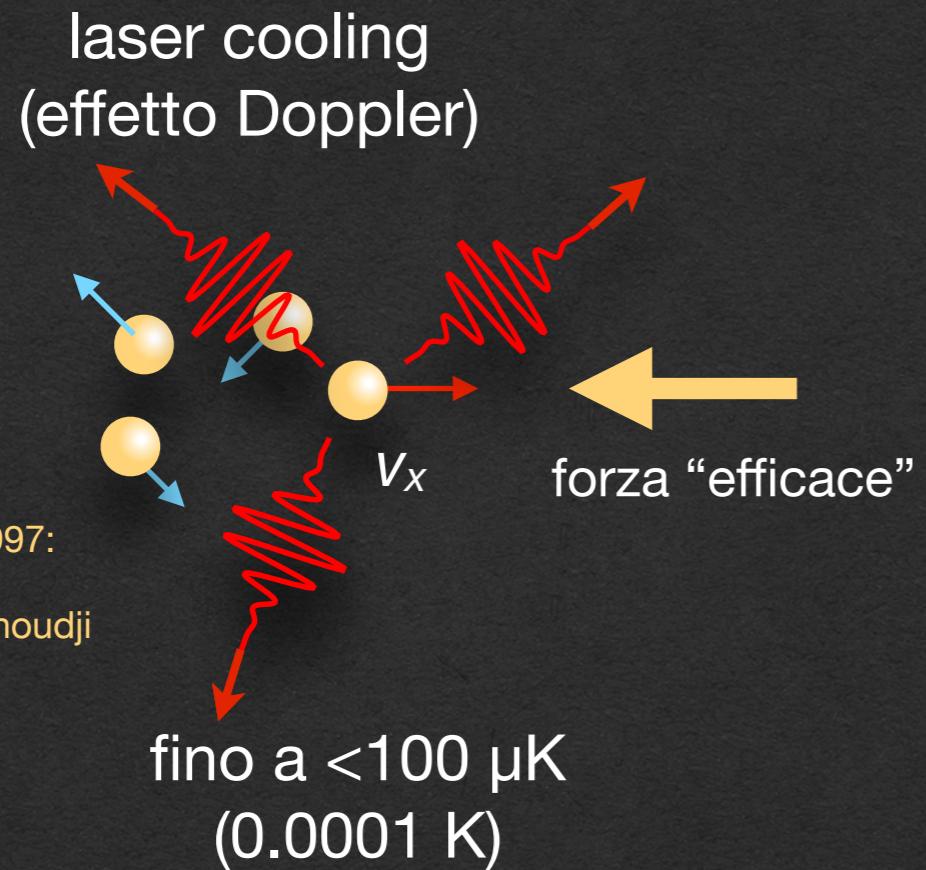


# vicini allo zero assoluto!

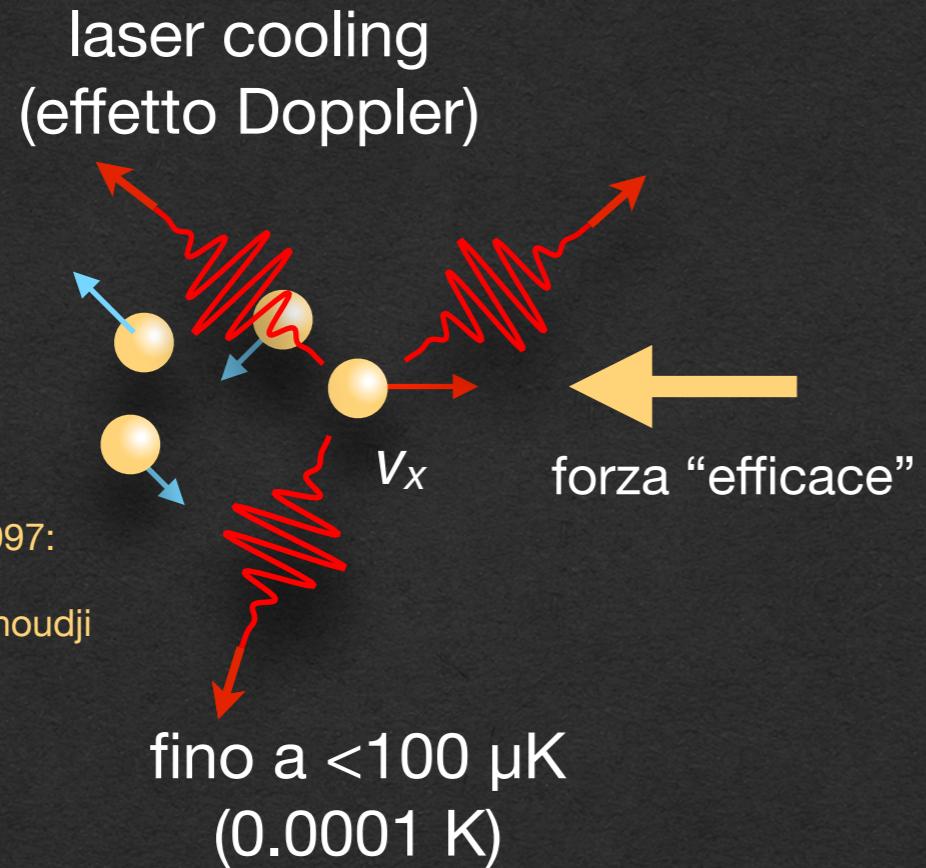
laser cooling  
(effetto Doppler)  $\nu' = \nu(1 + \frac{v_x}{c})$



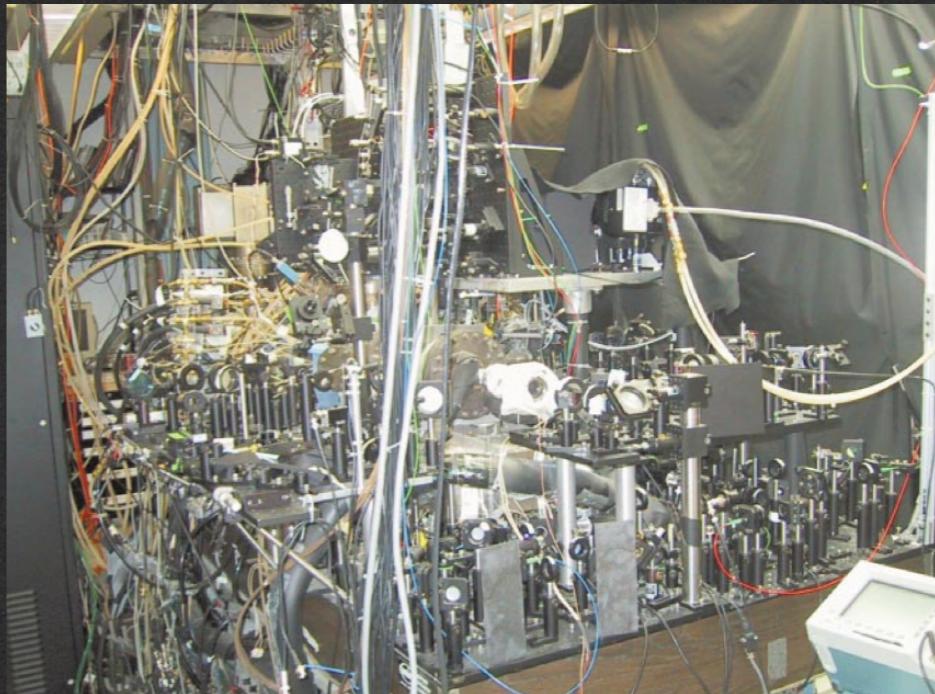
# vicini allo zero assoluto!



# vicini allo zero assoluto!

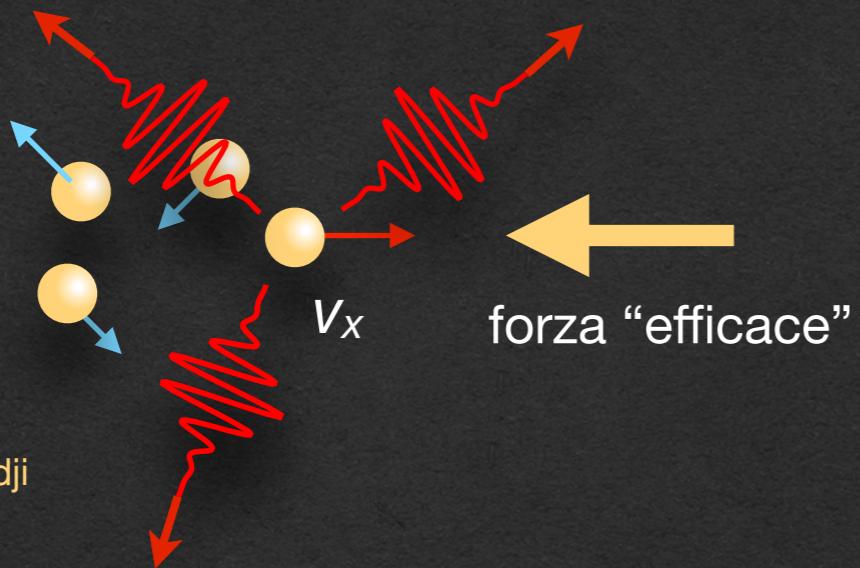


W. Ketterle Nobel Lecture 2001



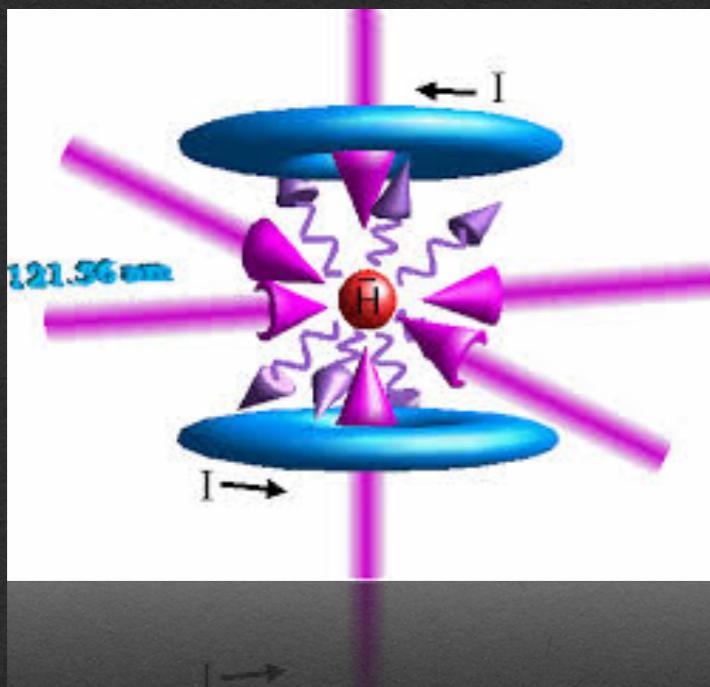
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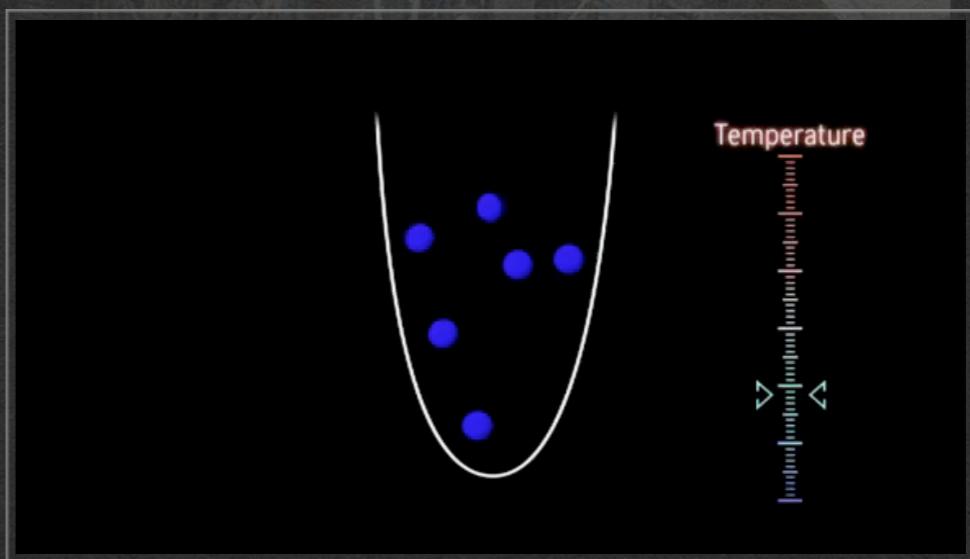
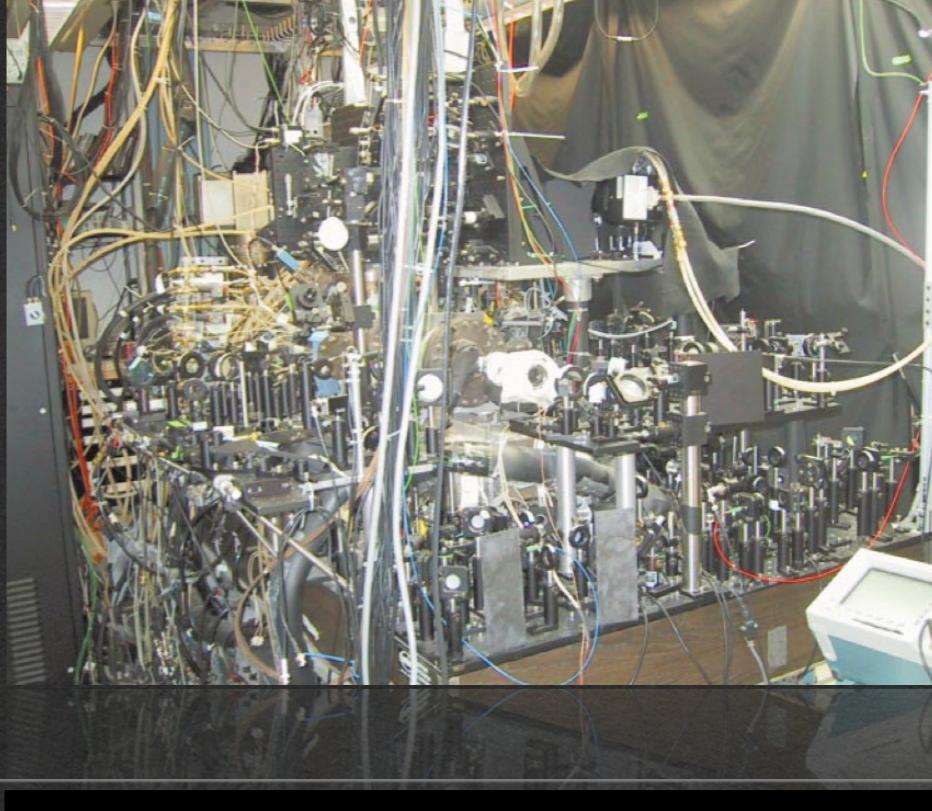


Nobel Prize 1997:  
S. Chu  
C. Cohen-Tannoudji  
W.D. Phillips

trappola magnetica e evaporazione

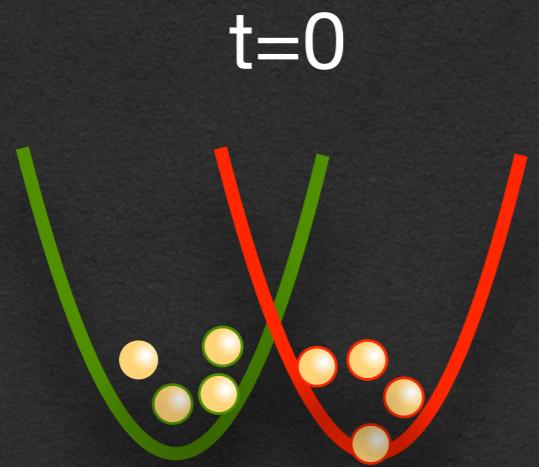


fino a  $<1 \mu\text{K}$   
( $0.000001 \text{ K}$ )

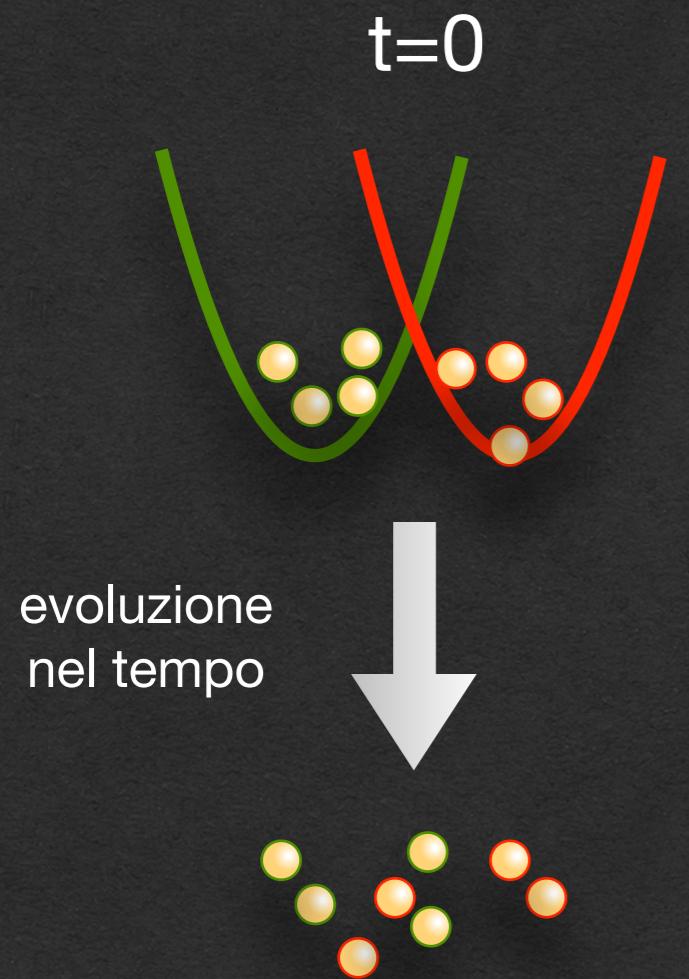


# materia come onde

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# materia come onde



onde o particelle?



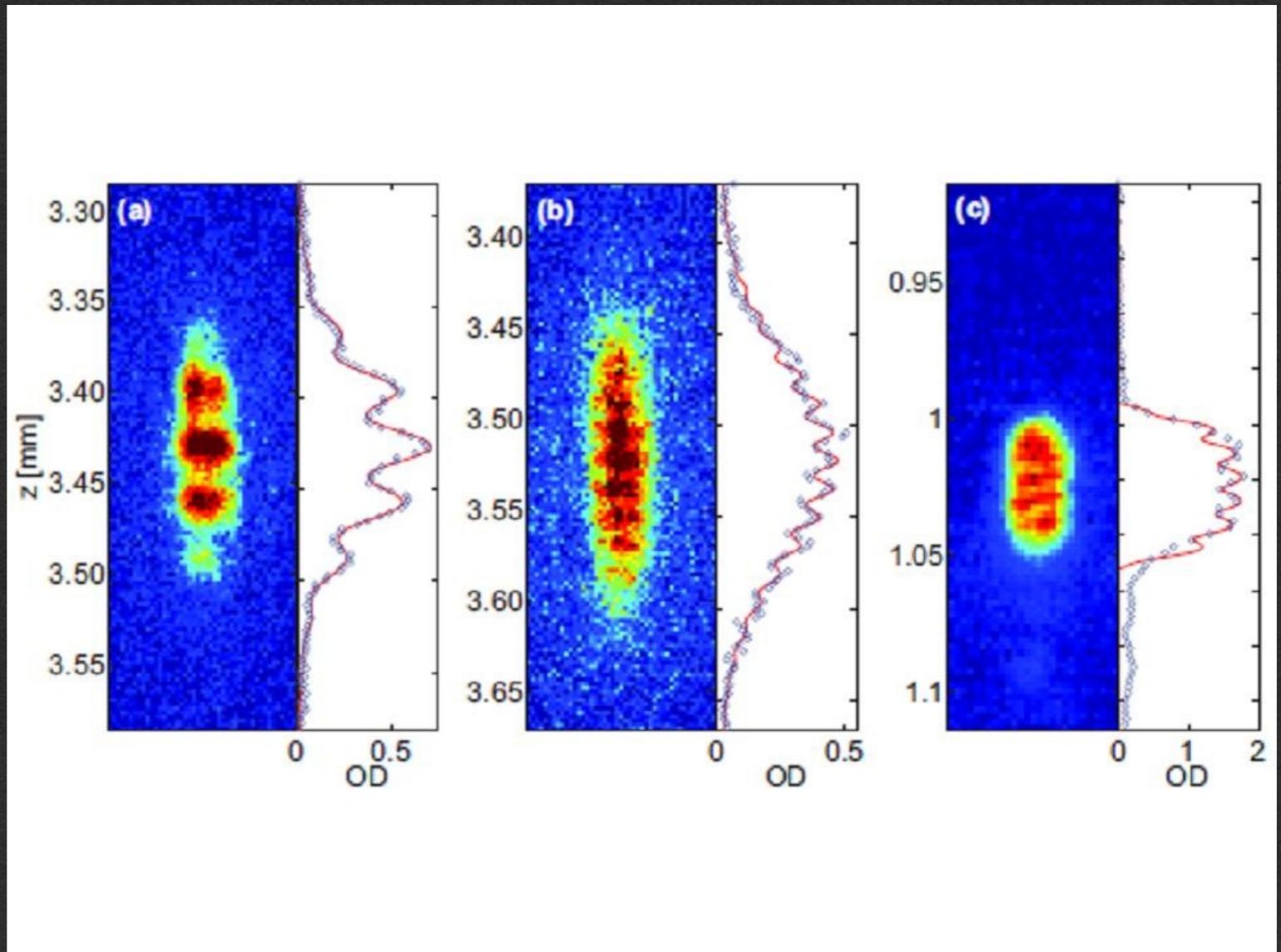
# materia come onde

$t=0$

evoluzione  
nel tempo



interferenza di materia!!



onde o particelle?

Ben Gurion University 2012



# vortici di materia

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Nobel Prize 2003:  
A.A. Abrikosov  
V.L. Ginzburg  
A.J. Leggett



reticolli di vortici  
di materia in  
condensati

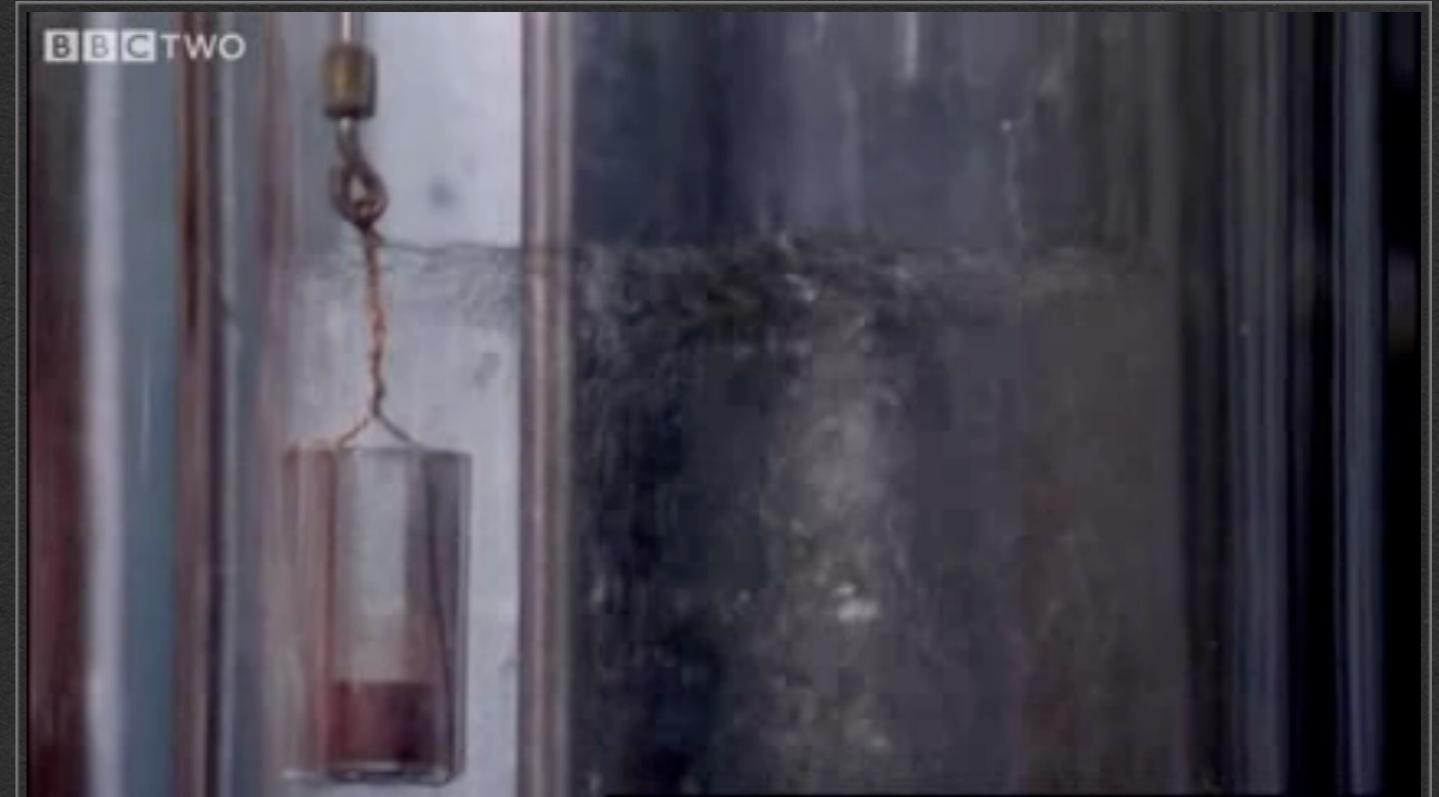
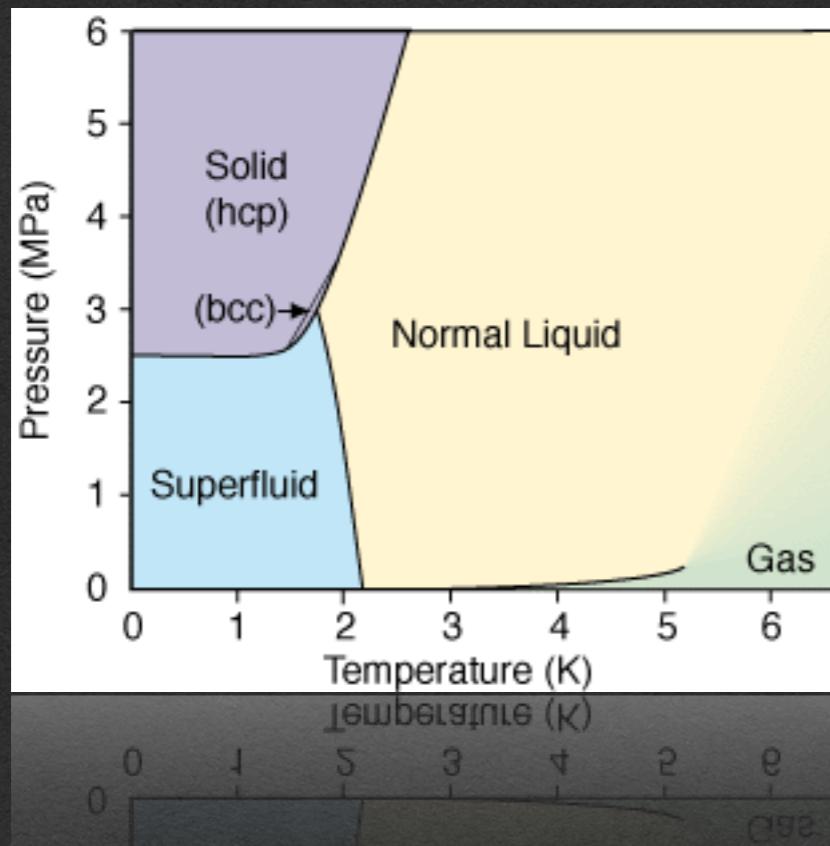


- 
- Condensazione di Bose-Einstein
  - Superfluidità  
(scoperta negli anni '30 da Kapitza, Nobel Prize 1978)
  - Supercondutività



# $^4\text{He}$ superfluido

diagramma delle fasi di  $^4\text{He}$ :  
l'unico liquido quantistico!



superfluidità a  $T < T_c = 2.17 \text{ K}$

- no viscosità
- singolo stato quantistico
- vortici

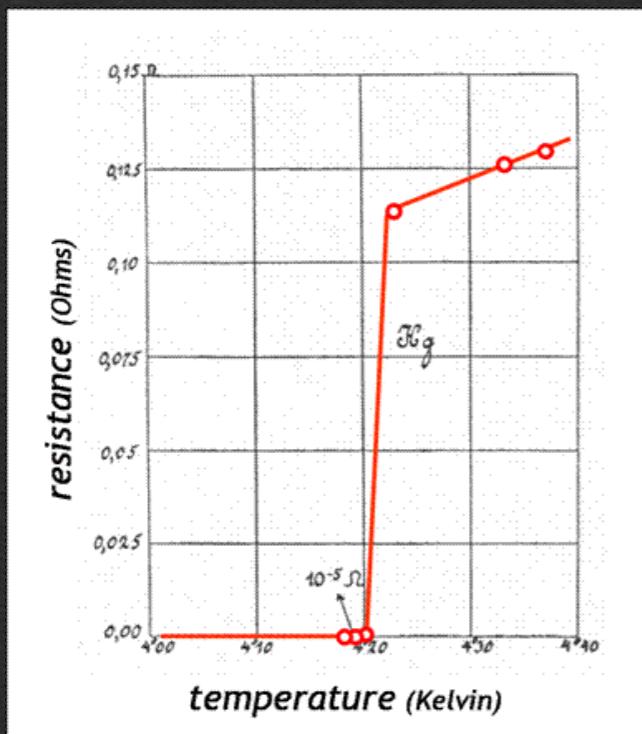


- 
- Condensazione di Bose-Einstein  
(predetta nel 1925 → scoperta in atomi alkalini nel 1995)
  - Superfluidità
  - Superconduttività  
(scoperta nel 1911 → capita nel 1972 (BCS)  
→ superconduttività ad alta temperatura 1986)

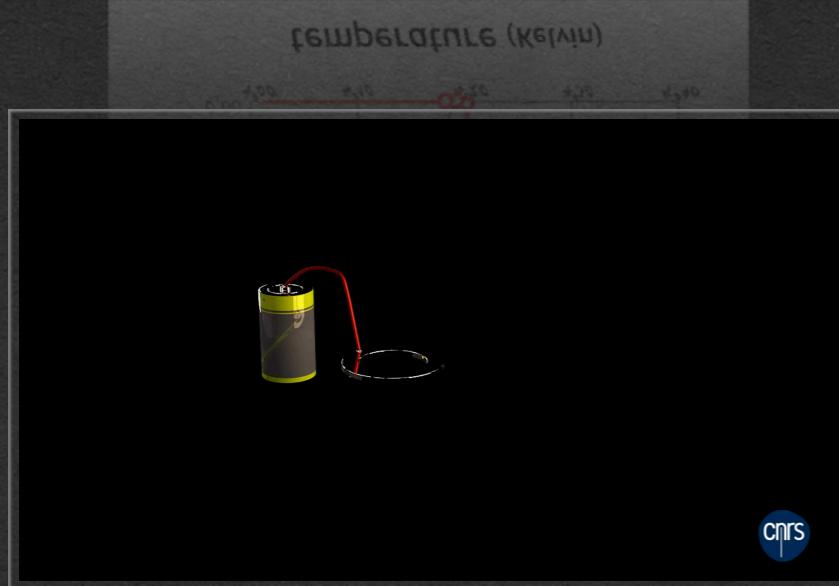


# supercondutività

resistenza nulla



diff. potenziale  
 $V=R \cdot I$   
corrente



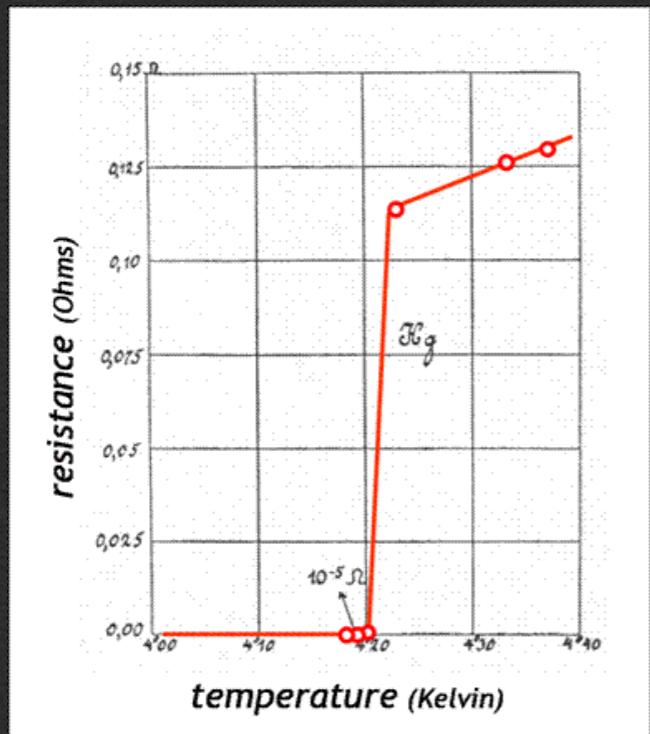
cnrs



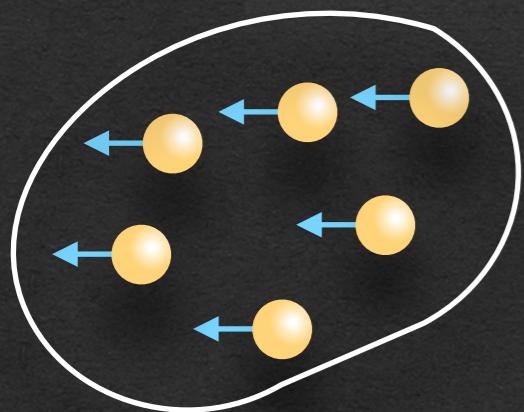
# supercondutività

resistenza nulla

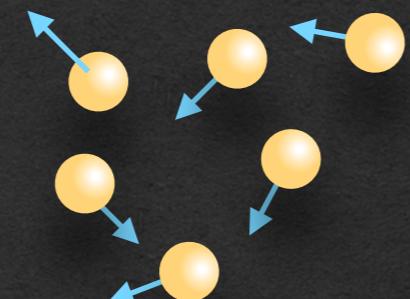
Nobel Prize  
1913:  
K. Onnes



moto collettivo



moto casuale e urti

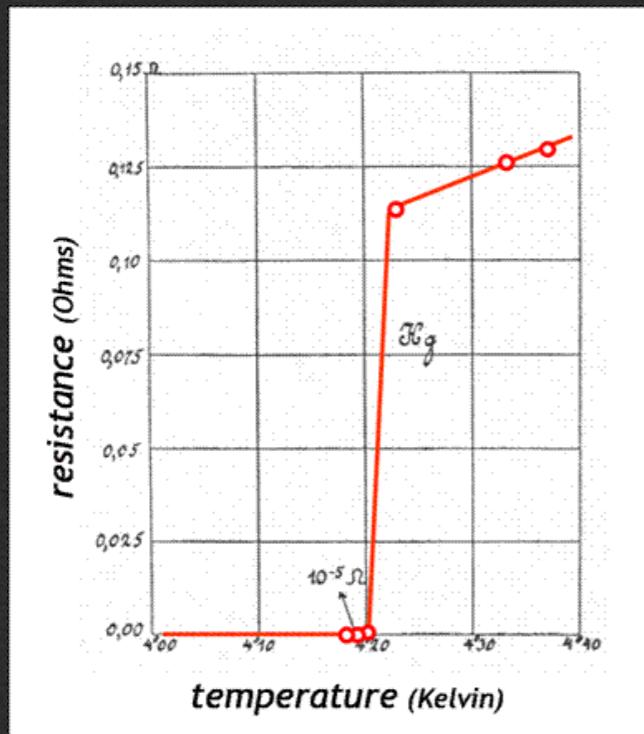


$$T_c = 4.2 \text{ K} @ \text{Hg}$$



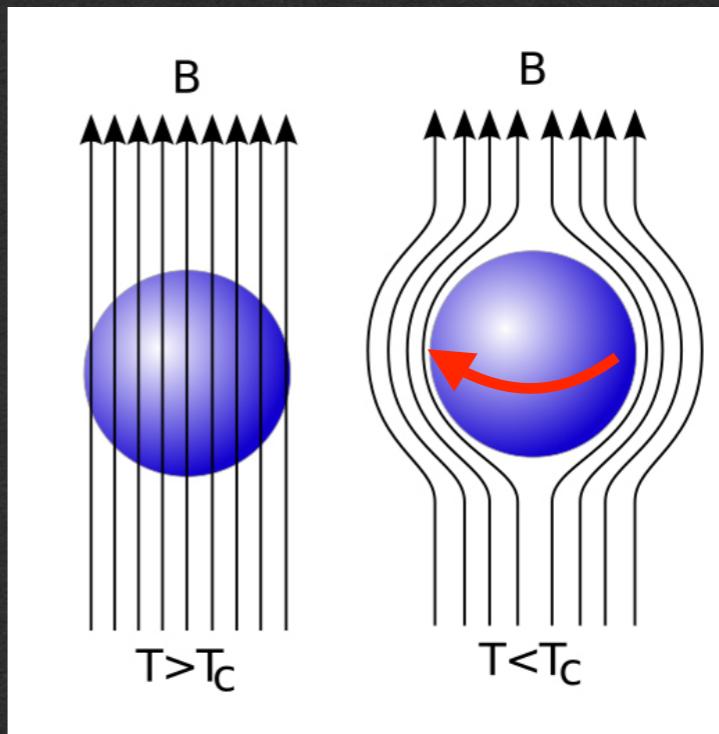
# superconduttività

resistenza nulla



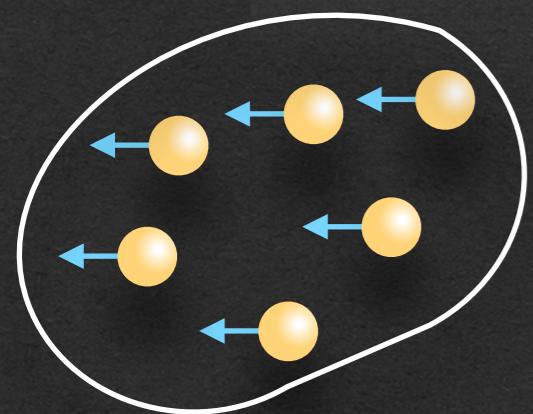
Nobel Prize  
1913:  
K. Onnes

repulsione di campi magnetici

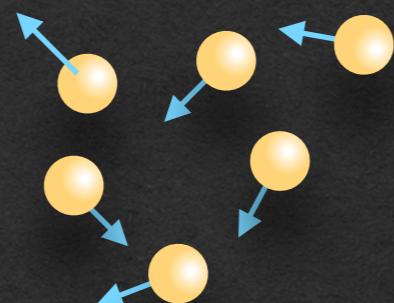


supercorrenti

moto collettivo



moto casuale e urti

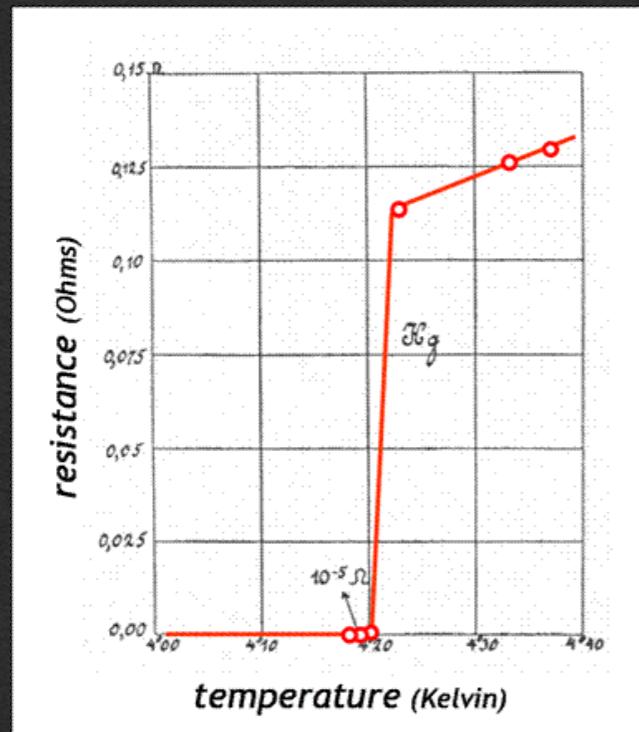


$T_c = 4.2 \text{ K} @ \text{Hg}$



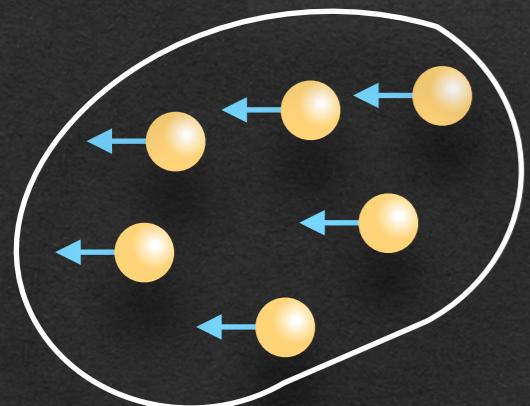
# superconduttività

resistenza nulla

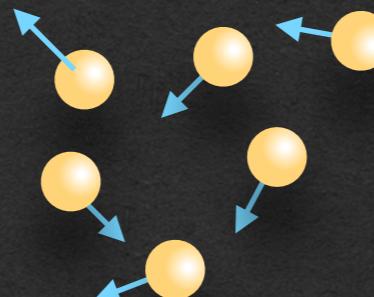


Nobel Prize  
1913:  
K. Onnes

moto collettivo

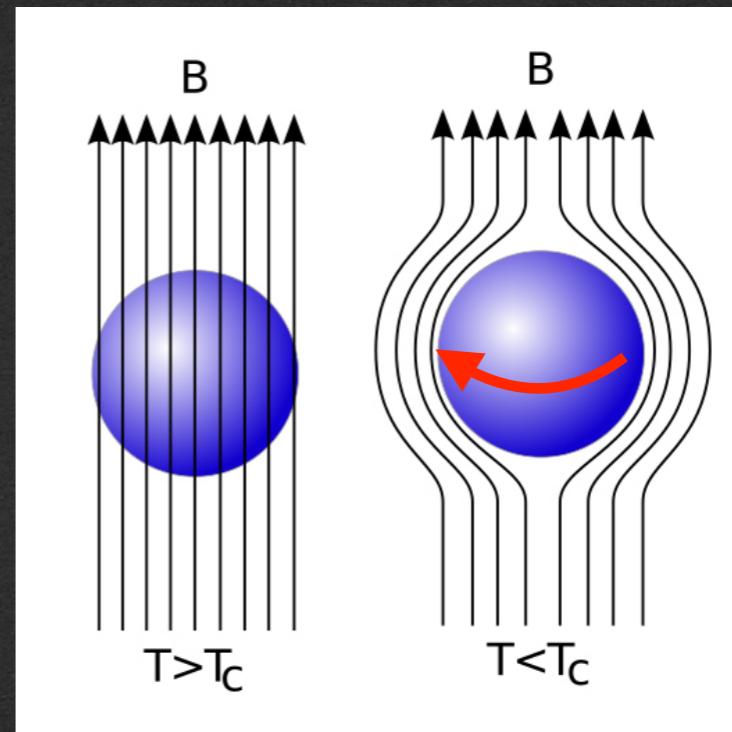


moto casuale e urti



$T_c = 4.2 \text{ K}$  @ Hg

repulsione di campi magnetici



supercorrenti

$T > T_c$        $T < T_c$   
fenomeno universale!

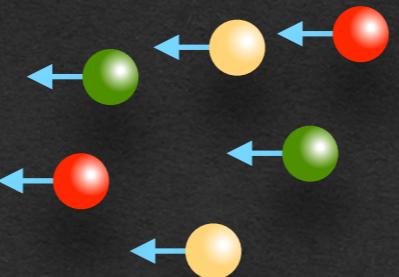
Superconducting Elements																	
In Bulk at Ambient Pressure												At High Pressure					
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
H	He	Li	Be	B	C	N	O	F	Ne	Na	Mg	Al	Si	P	S	Cl	Ar
2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Ti	Pb	Bi	Po	At	Rn
87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104
Fr	Ra	Ac	Rf	Ha	Sg	Bh	Hs	Mt	Ds	Uub	Ce	Pr	Nd	Pm	Sm	Eu	Lu
90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cr	Es	Fm	Md	No	Lr				



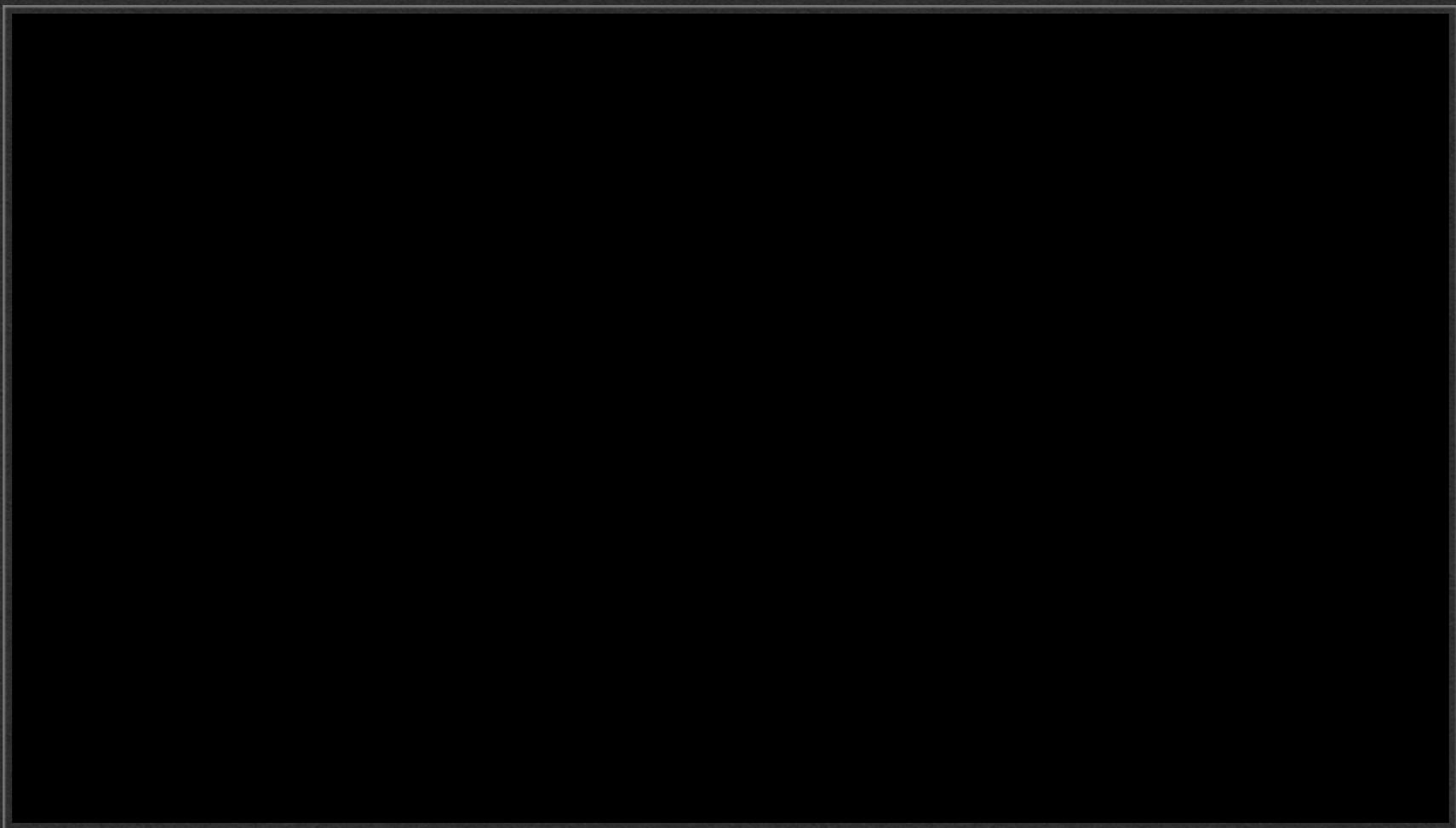
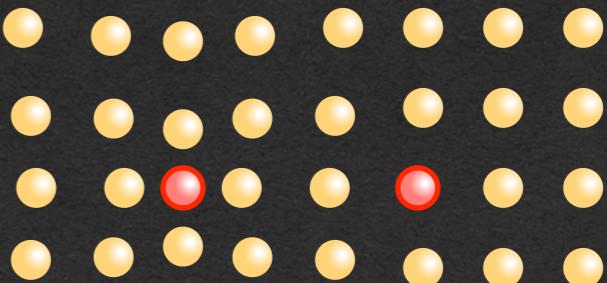
# superconduttività

teoria BCS →  
(Nobel Prize 1972)

formazione di coppie di e<sup>-</sup>  
(bosoni) e condensazione



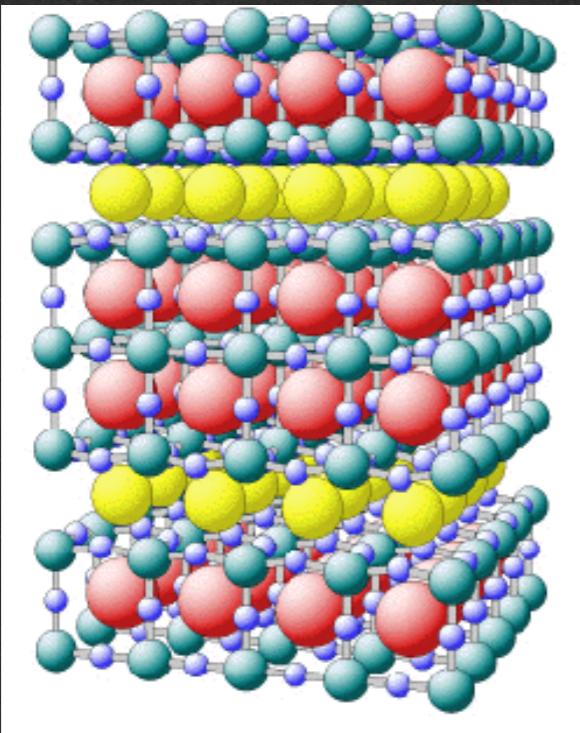
distorsione del  
reticolo cristallino



# superconduttività ad alta temperatura

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ossidi di metalli di  
transizione (Cu)  
bidimensionali

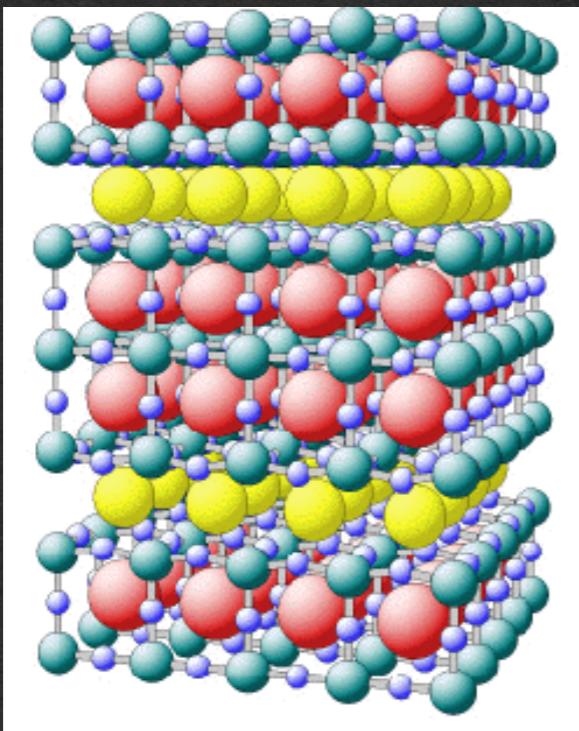


Nobel Prize 1986:  
J.G. Bednorz, K.A. Müller



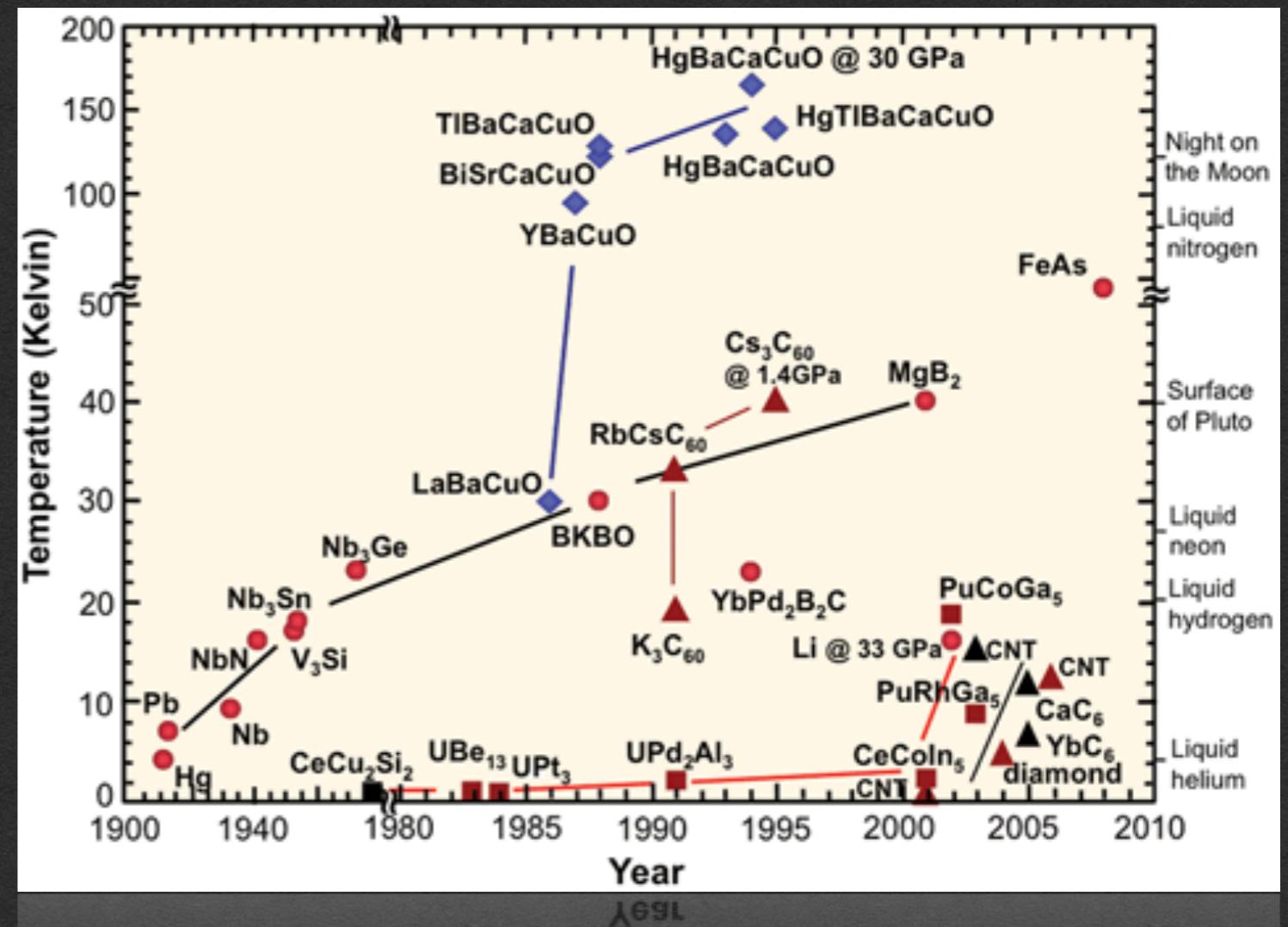
# superconduttività ad alta temperatura

ossidi di metalli di transizione (Cu) bidimensionali



Nobel Prize 1986:  
J.G. Bednorz, K.A. Müller

T<sub>c</sub> fino a 160 K !!

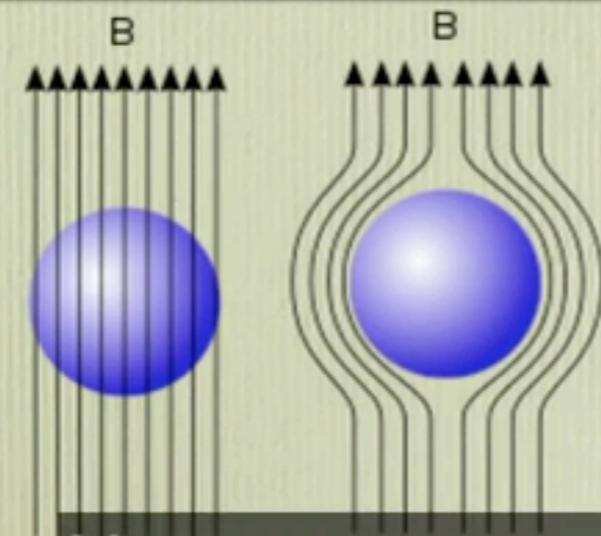


# superconduttività ad alta temperatura

What defines a SUPERCONDUCTOR?

SUPERCONDUCTOR will have both :

**expulsion of magnetic fields**



Ma, come sappiamo, nulla è perfetto

**Zero electrical resistance.**



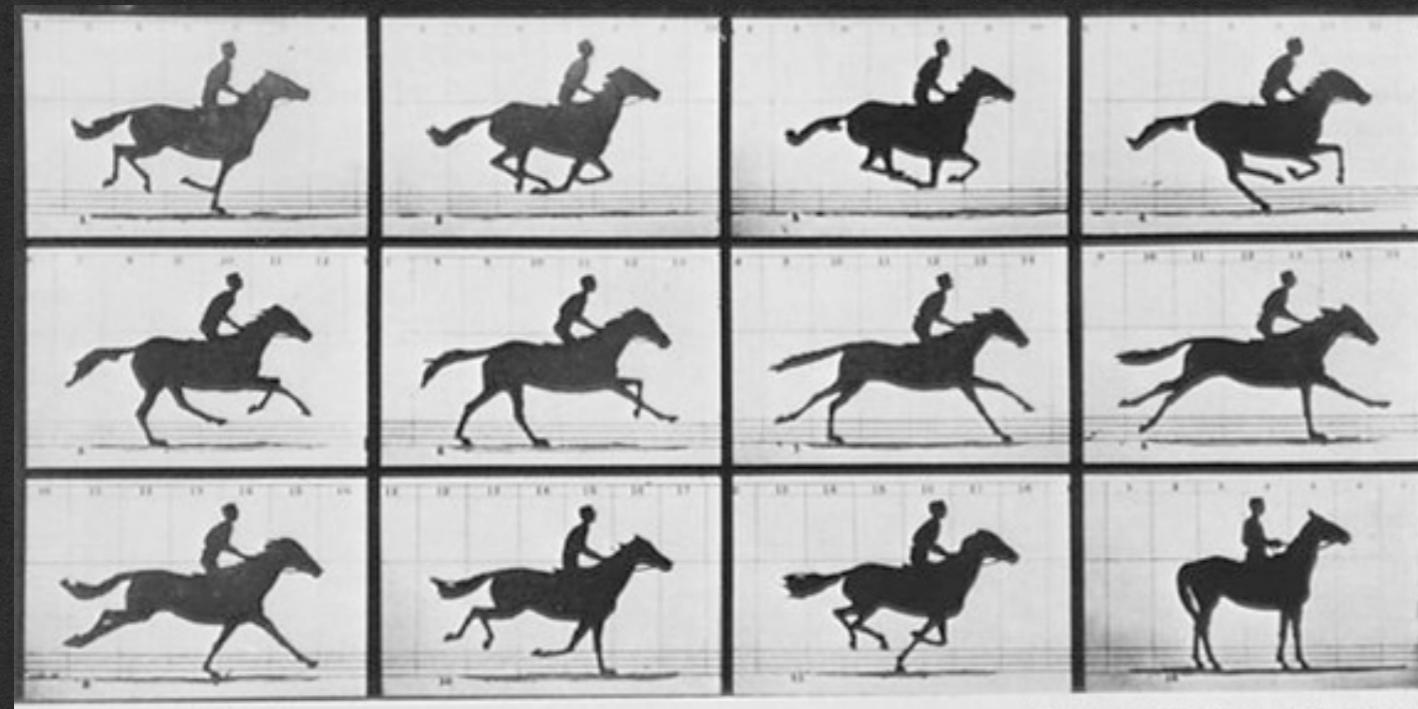
---

cosa facciamo noi?



# ottica ultraveloce

Fotografia stroboscopica ad alta velocità E. Muybridge (1872, San Francisco)



Copyright, 1878, by MUYBRIDGE.

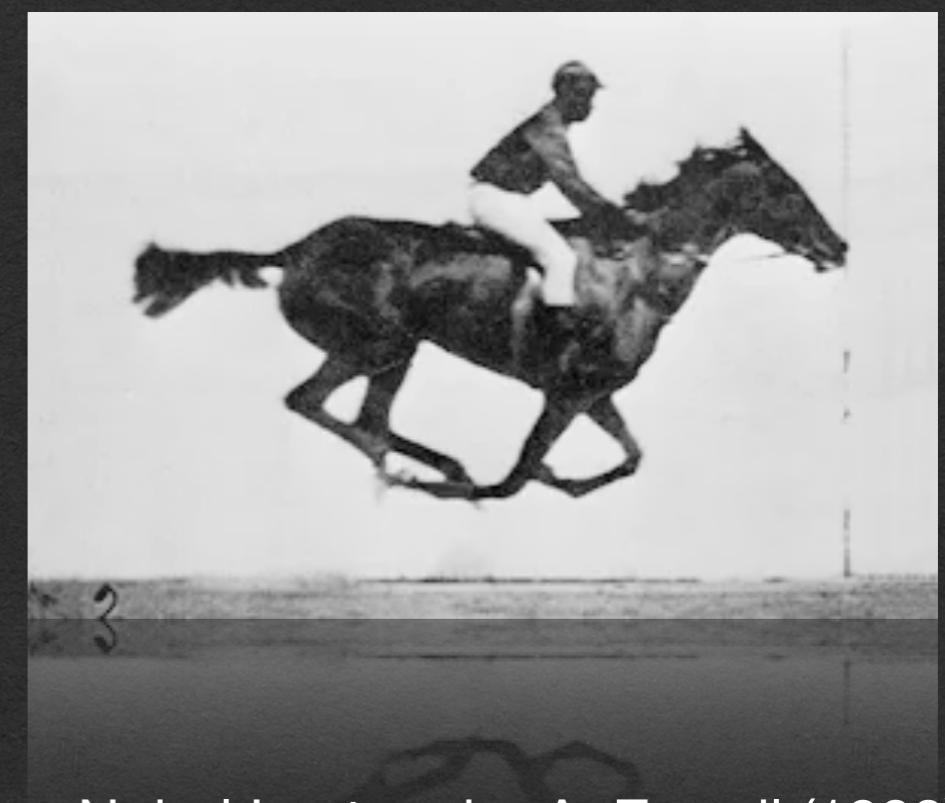
## THE HORSE IN MOTION.

Illustrated by  
MUYBRIDGE.

"SALLIE GARDNER," owned by LELAND STANFORD; running at a 1.40 gait over the Palo Alto track, 19th June, 1878.

AUTOMATIC ELECTRO-PHOTOGRAPHIC

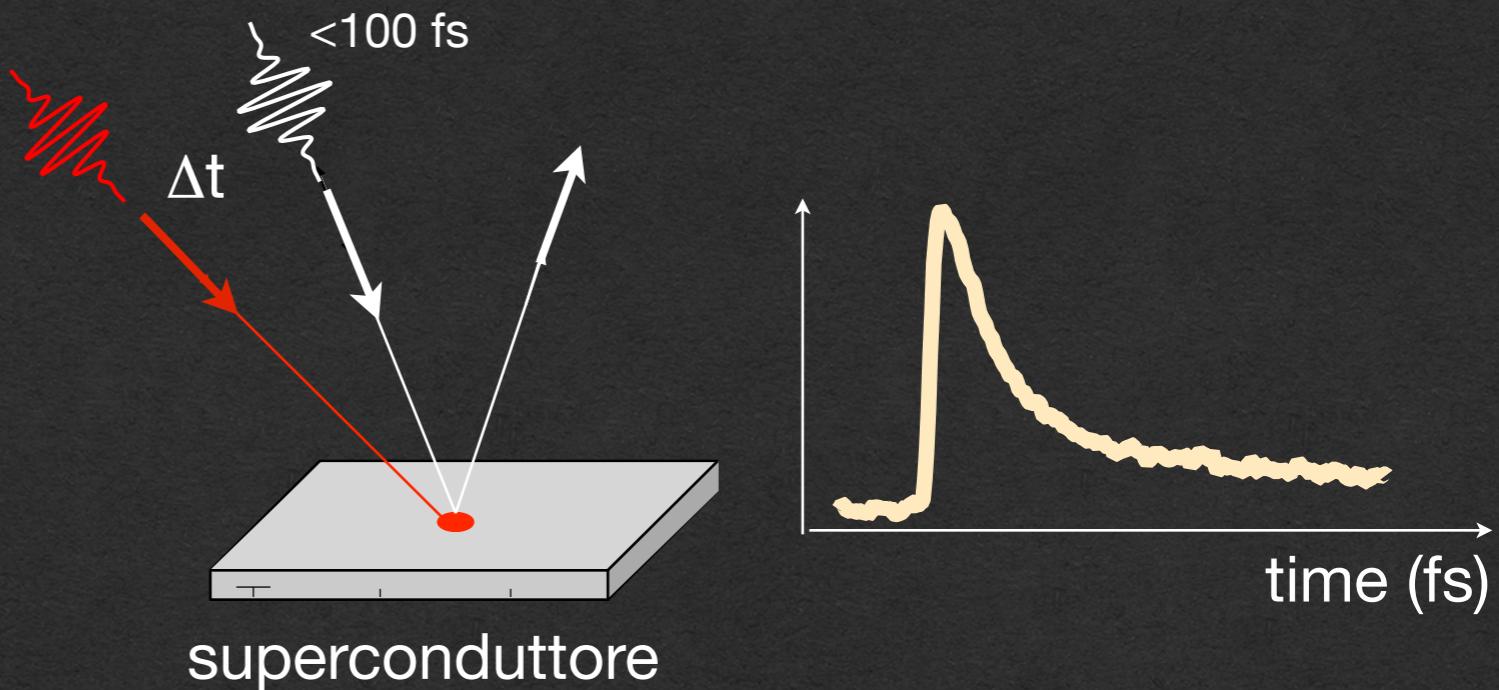
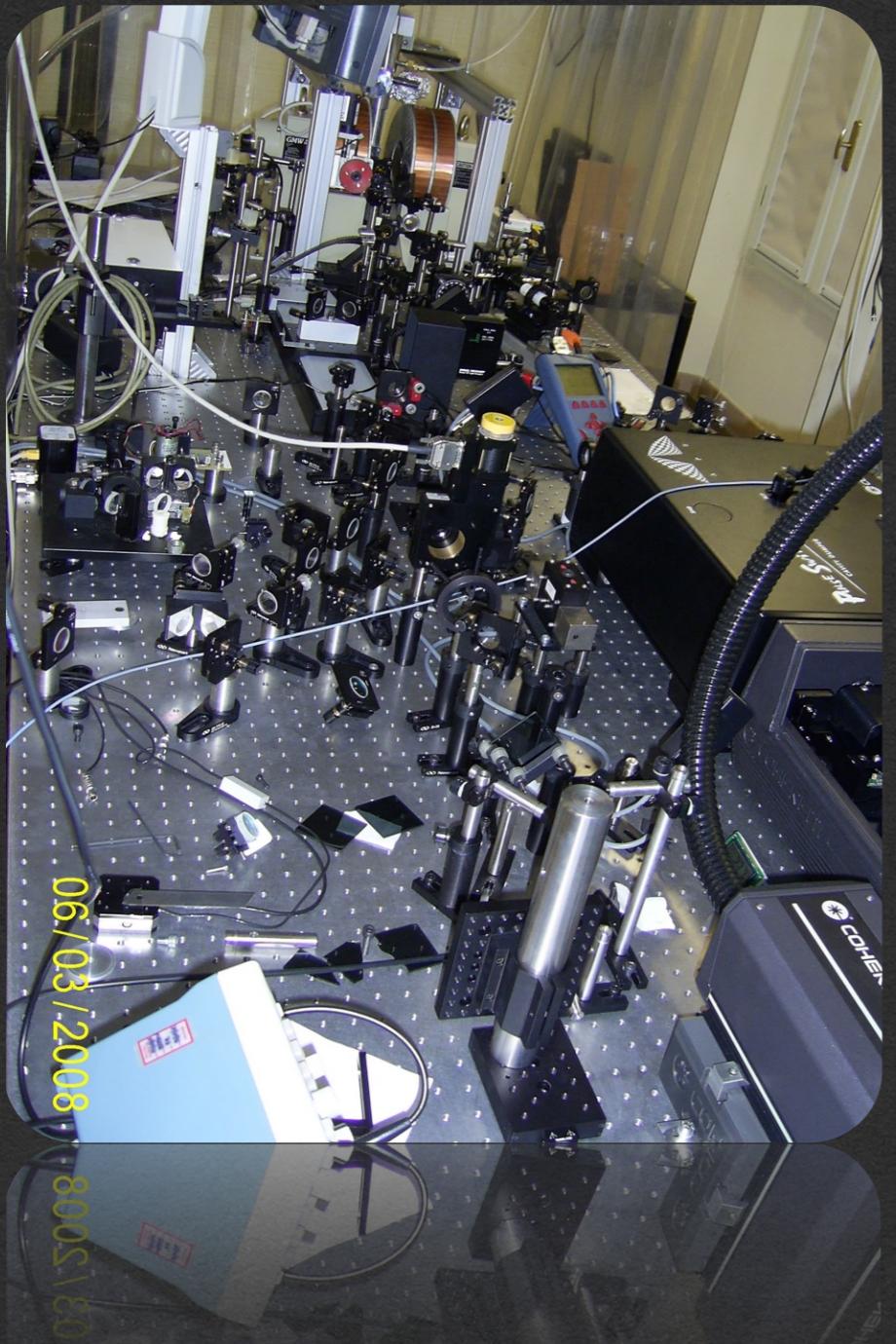
shutter ultraveloce?



Nobel Lecture by A. Zewail (1999)



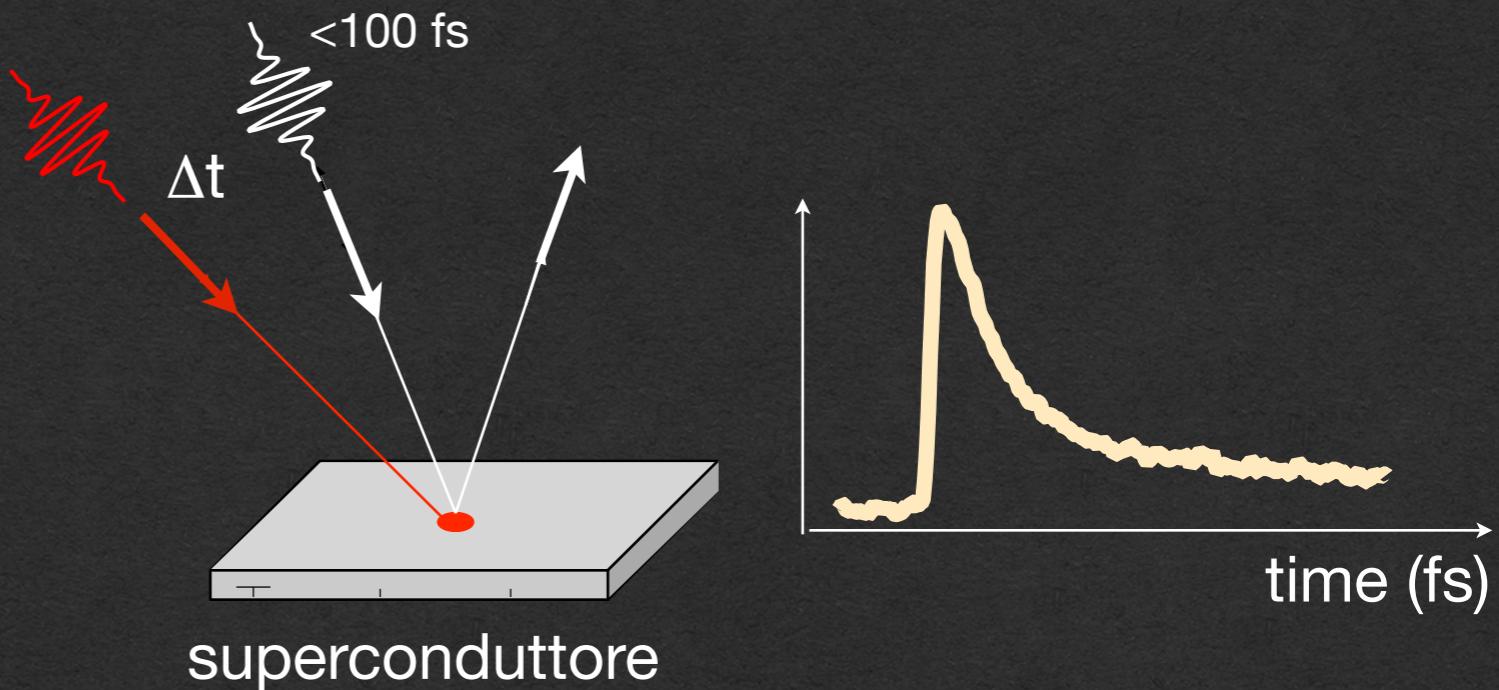
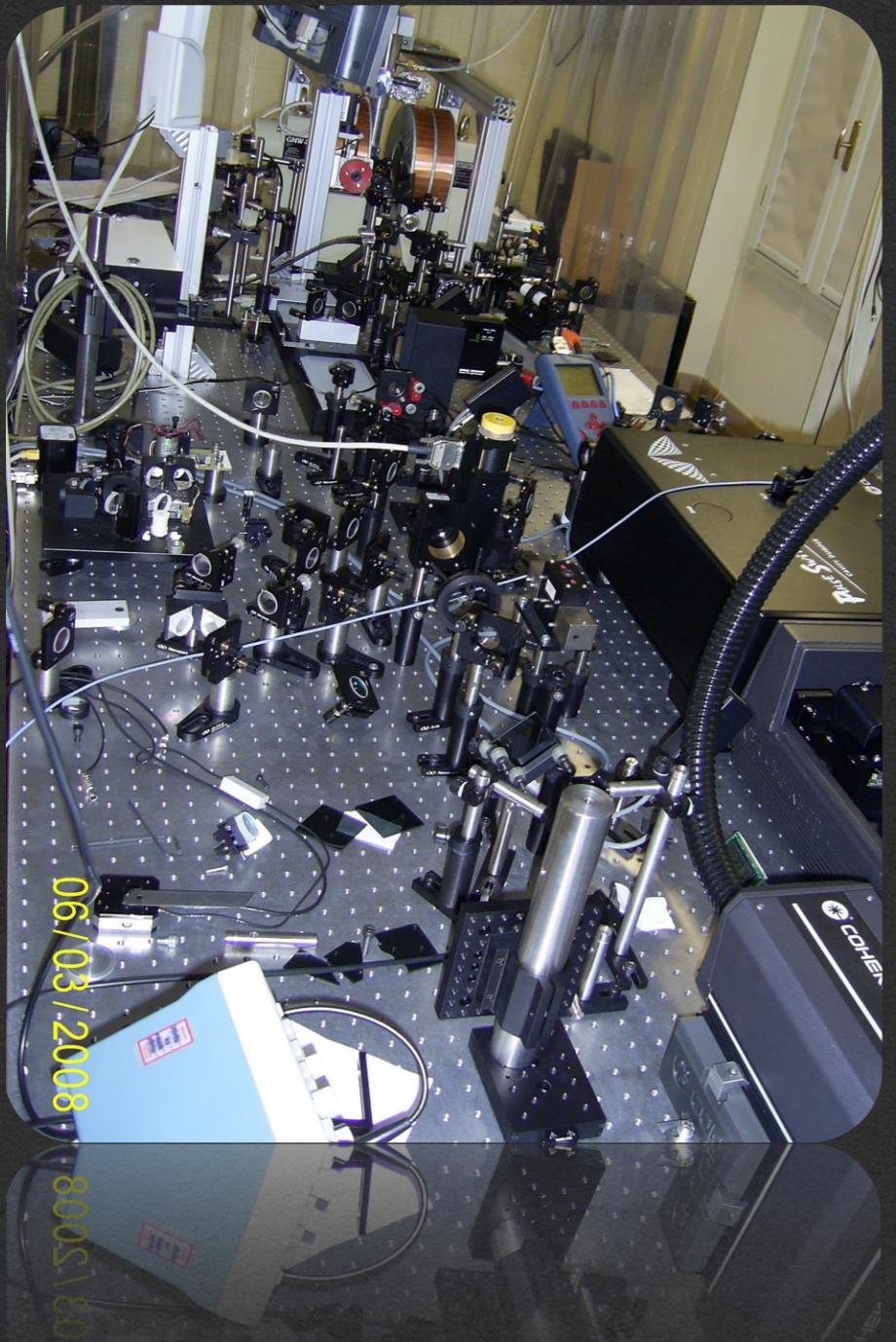
# Time-resolved optical spectroscopy



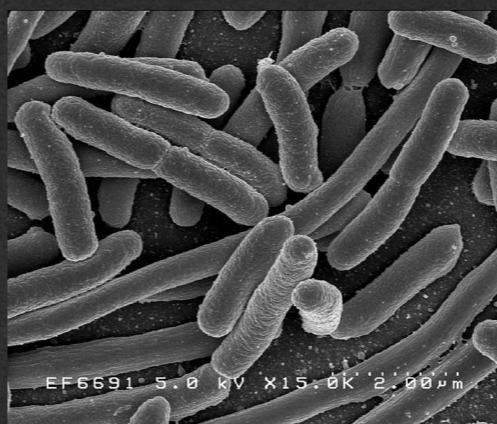
1 femtosecondo =  $10^{-15}$  s



# Time-resolved optical spectroscopy



1 femtosecondo =  $10^{-15}$  s



batterio



terra-luna



sei interessato?

*Interdisciplinary laboratories for  
advanced materials physics  
(I-LAMP)*

<http://centridiricerca.unicatt.it/ilamp>

